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## Tools, Proofs \& Transversals Quarter 1 Review 1

1. Part of a proof is shown. Place statements and reasons in the table to complete the proof.

Given $\overline{L E} \cong \overline{M R}, \overline{E G} \cong \overline{R A}$
Prove $\overline{L G} \cong \overline{M A}$


Statement
Reason
a. $\overline{L E} \cong \overline{M P}, \overline{E G} \cong \overline{R A}$
b. $\quad L E=M R$

$$
E G=R A
$$

c. $\quad L G=L E+E G$
$M A=M R+R A$
d. $\quad L G=M R+R A$
e. $L G=M A$
f. $\overline{L G} \cong \overline{M A}$

## 2021 Question 37

A diagram is shown, where $k \| I$ and $m$ is a transversal.


Move statements and reasons to the table to prove that $\angle 1 \cong \angle 5$.

| Statements | Reasons |
| :--- | :--- |
| 1. $k \\| I$ | 1. Given |
| 2. $\angle I \cong L 3$ | 2. Corresponding angles <br> are congruent. |
| 3. $\angle 3 \cong 2 S$ | 3. Vevtical angles are cungruent |
| 4. $\angle 1 \cong \angle 5$ | 4. Transifive Preperty |


| $\angle 1 \cong \angle 2$ | $\angle 1 \cong \angle 3$ | $\angle 1 \cong \angle 4$ |
| ---: | :--- | ---: |$\quad \angle 2 \cong \angle 3$

Transitive property Symmetric property
Vertical angles are congruent.
Straight angles form a linear pair.
Corresponding angles are congruent.
Alternate exterior angles are congruent.
2. Which term is defined as an angle formed by two opposite rays?
A. Straight angle
B. Vertical angle
C. Corresponding angle
D. Complementary angle
3. Kevin asked Olivia what the Supplement Theorem is. Olivia responded, " $m \angle 1+$ $m \angle 2=180$." What definition did Olivia actually give?
A. Definition of a straight angle
(B) Definition of supplementary angles
C. Definition of complementary angles
D. Definition of transversal
4. Jeremy wants to know the density of a rock in grams per cubic centimeter. The rock has a mass of 4.45 kilograms and a volume of 508 cubic centimeters.
What is the density of the rock, in graphs per cubic centimeter $\left(\frac{g}{\mathrm{~cm}^{3}}\right)$ ?

5. Line $\boldsymbol{k}$ has a slope of 4 . Line $\boldsymbol{j}$ is perpendicular to line $\boldsymbol{k}$ and passes through the point $(-2,8)$. Create the equation for line

6. $\overline{A C}$ has endpoints $\mathrm{A}(-1,-\bar{X})$ and $\mathrm{C}(5, \mathcal{X})$. Point B is on $\overline{A C}$ and is located at $(0.2, X)$. What is the ratio of $\frac{A B}{B C}$ ?

ne hod 2
$\begin{array}{rlrl}A B & =\sqrt{[\Delta x]^{2}+[\Delta y]^{2}} & B C & =\sqrt{[\Delta x]^{2}+[\Delta y]^{2}} \\ & =\sqrt{[-1-0.2]^{2}+[-3.5-(-3)]^{2}} & =\sqrt{[(5)-(0.2)]^{2}+[(-1)-(-3)]^{2}} \\ & =\sqrt{[-1.2]^{2}+[0.5]^{2}} & & =\sqrt{[4.8]^{2}+[\partial]^{2}} \\ & =\sqrt{1.44+0.25} & & =\sqrt{23.04+4} \\ & =\sqrt{1.69} & & =\sqrt{27.04} \\ A B & \approx 1.3 & B C & =5.2\end{array}$
$B C=5.2$

$$
\frac{A B}{B C} \simeq \frac{1.3}{5.2}=\frac{1}{4}
$$

7. A study reports that in 2010 the population of the United States was $308,745,538$ people and the land area was approximately 3,531,905 square miles.
Based on the study, what was the
porfulation density, in people per square mile, of the United States in 2010? Round your answer to the nearest tenth.

$$
87.4
$$

people per
square mile
$\frac{308,245,538 \text { people }}{3.531,905 \text { mile }} \approx 87.4 \mathrm{p} / \mathrm{mi} i^{2}$
$\qquad$
8. Square $A B C D$ has vertices at $A(1,2)$ and $B(3,-3)$. What is the slope of $\overline{B C}$ ?


$$
\begin{aligned}
m \overline{A B} & =\frac{\Delta y}{\Delta x}=\frac{2-(-3)}{1-3}=\frac{5}{-2} \\
m \overline{B C} & =1 m \overline{A B}=2 / 5
\end{aligned}
$$

9. The graph of line $m$ is shown


What is the equation of the line that is perpendicular to line $m$ and passes through the point ( $-2,4$ )?

$$
\begin{aligned}
& \frac{\text { Point }}{(-2,4)} \frac{\text { slope }}{m}=-4 / 3 \begin{array}{l}
\text { Point-slope for } \\
y-y_{1}=m\left(x-x_{1}\right) \\
\perp m=\frac{3}{4}
\end{array} \\
& y-4=\frac{3}{4}(x+2)
\end{aligned}
$$

10. Point $A$ is located at $(4,-3)$. The midpoint of line segment $A B$ is point $C(1,2)$. What are the coordinates of point B ?

op mom 2

- $B(-2,7) \in A$ assures


2018 Question 15
Square $A B C D$ has vertices at $A(1,2)$ and $B(3,-3)$. What is the slope of $\overline{B C}$ ?


$$
\begin{aligned}
& m_{\overline{A B}}=\frac{5}{-2} \\
& m_{\overline{B C}}=1 m_{\overline{A B}}=\frac{2}{5}
\end{aligned}
$$

## 2017 QUESTION 16

Kevin asked Olivia what parallel lines are. Olivia responded, "They are lines that never intersect." What important piece of information is missing from Olivia's response?
e. The lines must be straight.
g. The lines can be noncoplanar.
h. The lines form four right angles.

## 2018 Question 39

Part of a proof is shown. Place statements and reasons in the table to complete the proof.
Given: $m \| n$ and transversal $p$
Prove: $\angle 5 \cong \angle 4$



| $\angle 8 \cong \angle 1$ | Vertical angles theorem |
| :--- | :--- |
| $\angle 1 \cong \angle 4$ | Corresponding angles postulate |
| $\angle 8 \cong \angle 4$ | Transitive property |
| $\angle 5 \cong \angle 8$ | Alternate exterior angles theorem |
| $\angle 5 \cong \angle 7$ | Reflexive property |
| $\angle 4 \cong \angle 7$ | Angle addition postulate |

$\qquad$
Tools, Proofs \& Transversal
Quarter 1 Review 2

1. Part of a proof is shown. Place statements and reasons in the table to complete the proof.

Given $\angle 1 \cong \angle 3$

Prove

$$
\angle 2 \cong \angle 4
$$

a. $\angle 1 \cong \angle 3$
b. $m L I=m L 3$
$\angle 1$ and $\angle 2$ are linear pair
c. $\angle 3$ and $\angle 4$ are linear pair
$\angle 1$ and $\angle 2$ are Supplementary
d. $\angle 3$ and $\angle 4$ are Supplementary
e.

$$
m \angle 1+m \angle 2=180^{\circ}
$$

$m \angle 3+m \angle 4=180^{\circ}$
f.

$$
m \angle 1+m \angle 2=m \angle 3+m \angle 4
$$

g.

$$
m \angle 3+m \angle 2=m<3+m \angle 4
$$

$$
m \angle \partial=m \angle 4
$$

h.

$$
\angle 2 \cong \angle 4
$$

ii.

Reason
a. GIVEN

Devin of Congrats Angles
Detain of linear pair
c. Supplement Theorem
d.
$\qquad$
e. $\qquad$ Subs Po E
f. subst. PoE
g. $\qquad$ Subtr. POE
h. Defer of Cargmat Angles
i. $\qquad$
2. Which term is defined as nonadjacent angles formed by two intersecting lines?
A. Straight angle
B. Vertical angle
C. Corresponding angle
D. Complementary angle
3. Kevin asked Olivia what the Alternate Interior Angles Theorem is. Olivia responds, "When a transversal intersects two lines, the alternate interior angles are congruent." What is wrong with Olivia's responds?
A. She should have said the alternate interior angles are supplementary, instead of congruent.
B. She should have said the alternate interior angles are complementary, instead of congruent.
C. She should have said the transversal intersects two parallel lines.
D. She should have said the transversal intersects two perpendicular lines.
4. Jeremy wants to know the density of a pop tart in grams per cubic centimeter. The pop tart has a mass of 0.00183 kilograms and a volume of 97 cubic centimeters.
What is the density of the pop tart, in graphs per cubic centimeter $\left(\frac{g}{c m^{3}}\right)$ ?


5. Line $\boldsymbol{k}$ has a slope of $-\frac{2}{3}$. Line $\mathfrak{j}$ is perpendicular to line $\boldsymbol{R}$ and passes through the point $(-4,-5)$. Create the equation for line $j$.

6. $\overline{A C}$ has endpoints $A(\underset{A}{ }$ 4) and $C(\mathbb{X})$. Point $B$ is on $\overline{A C}$ and is located at $(\mathbb{4}, 6)$. What is the ratio of $\frac{A B}{B C}$ ?

$\frac{A B}{B C}=\frac{2}{2}=1$
OR method 2
AB

$$
\begin{aligned}
B & =\sqrt{[\Delta x]^{2}+[\Delta y]^{2}} \\
& =\sqrt{[3-4.5]^{2}+[4-6]^{2}} \\
& =\sqrt{[-1.5]^{2}+[-2]^{2}} \\
& =\sqrt{2.25+4} \\
& =\sqrt{6.25}
\end{aligned}
$$

$$
A B=2.5
$$

$$
\begin{aligned}
B C & =\sqrt{[\Delta x]^{2}+[\Delta v]^{2}} \\
& =\sqrt{[6-4.5]^{2}+[8-6]^{2}} \\
& =\sqrt{[1.5]^{2}+[2]^{2}} \\
& =\sqrt{2.25+4} \\
& =\sqrt{6.25} \\
B C & =2.5
\end{aligned}
$$


7. A stpolyreports that in 2016 the population of the Gnaden was 1,283 people and the land area was approximately 0.96875 square miles.
Based on the study, what was the
population density, in people per square mile, of the United States in 2016? Round your answer to the nearest tenth.

$$
1324.4
$$ people per square mile

$\frac{1283 \text { people }}{0.96875 \mathrm{mi}^{2}} \approx 1324.4$
$\qquad$
8. Square $A B C D$ has vertices at $A(8,-2)$ and $B(5,-6)$. What is the slope of $\overline{C D}$ ?


$$
m \overline{A B}=\frac{\Delta y}{\Delta x}=\frac{-2-(-6)}{8-5}=\frac{4}{3}
$$

$$
\overline{C D} / / \overline{A B} \therefore m \overline{A B}=4 / 3
$$

9. The graph of line $m$ is shown


What is the equation of the line that is perpendicular to line $m$ and passes through the point (4, -2)?

$$
\begin{aligned}
& t_{m}=-3 / 2 \quad y+2=-\frac{3}{2}(x-4)
\end{aligned}
$$

10. Point A is located at $(-5,2)$. The midpoint of line segment $A B$ is point $C(1,-4)$. What are the coordinates of point B ?



Which term is defined as two intersecting lines that form four right angles in a plane?
a. Skew lines
b. Straight lines
c. Parallel lines
d. Perpendicular lines


2018 Question 9
Line $k$ has a slope of -5 . Line $j$ is perpendicular to line $k$ and passes through the point $(5,9)$. Create the equation for line $j$.


Point - Slope

$$
\begin{aligned}
& y-y_{1}=m\left(x-x_{1}\right) \\
& y-9=\frac{1}{5}(x-5) \in \text { Answer }
\end{aligned}
$$

## 2021 Question 22

A triangle JLM and line segment KN are given.


A proof of $\frac{J K}{J L}=\frac{J N}{J M}$ is shown.

| Statement | Reasons |
| :---: | :--- |
| $\Delta J L M$ | Given |
| $?$ | Given |
| $\angle J N K \cong \angle J M L$ |  |
| $\angle J K N \cong \angle J L M$ |  |$\quad$| Corresponding angles are congruent |
| :---: |
| we need paralle lines |

Which statement must be added to the given to keep this proof valid?
A. $\overline{J L} \perp \overline{L M}$
B. $\overline{K N} \perp \overline{L M}$
C. $\overline{J L} \| \overline{L M}$
D. $\overline{K N} \| \overline{L M}$

