

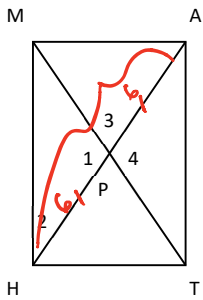
# Quadrilaterals – Rectangles

Homework Section 6.4

Name \_\_\_\_\_

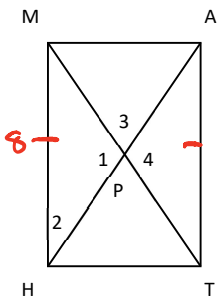
Use rectangle MATH and MNRS with the given information to solve each problem.

#1)  $HP = 6$ , find  $HA$



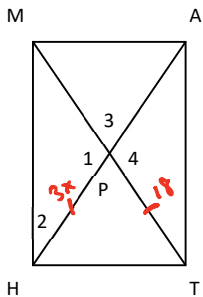
$$\begin{aligned} HP + PA &= HA \\ 6 + 6 &= HA \\ 12 &= HA \end{aligned}$$

#2)  $MH = 8$ , find  $AT$



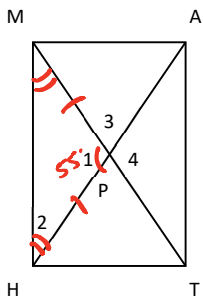
$$\begin{aligned} MH &= AT \\ 8 &= AT \end{aligned}$$

#3)  $HP = 3x$  and  $PT = 18$ , find  $x$



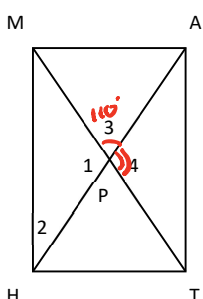
$$\begin{aligned} HP &= PT \\ 3x &= 18 \\ x &= 6 \end{aligned}$$

#4)  $m\angle 1 = 55$ , find  $m\angle 2$



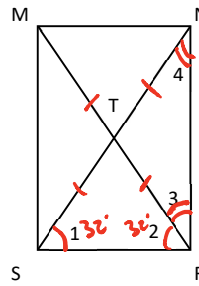
$$\begin{aligned} m\angle 1 + m\angle 2 + m\angle HMP &= 180 \\ 55 + m\angle 2 + m\angle 2 &= 180 \\ 55 + 2m\angle 2 &= 180 \\ 2m\angle 2 &= 125 \\ m\angle 2 &= \frac{125}{2} \end{aligned}$$

#5)  $m\angle 3 = 110$ , find  $m\angle 4$



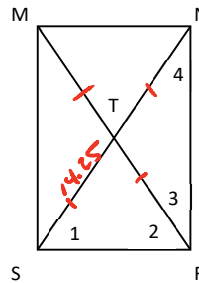
$$\begin{aligned} m\angle 3 + m\angle 4 &= 180 \\ 110 + m\angle 4 &= 180 \\ m\angle 4 &= 70 \end{aligned}$$

#6) If  $m\angle 1 = 32$ , find the  $m\angle 2$ ,  $m\angle 3$ , and  $m\angle 4$ .



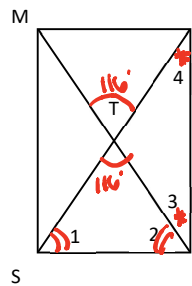
$$\begin{aligned} m\angle 2 &= 32 \\ m\angle 2 + m\angle 3 &= 90 \\ 32 + m\angle 3 &= 90 \\ m\angle 3 &= 58 \\ m\angle 3 &= m\angle 4 \\ 58 &= m\angle 4 \end{aligned}$$

#7) If  $ST = 14.25$ , find  $MR$



$$\begin{aligned} MR &= MT + TR \\ MR &= 14.25 + 14.25 \\ MR &= 28.5 \end{aligned}$$

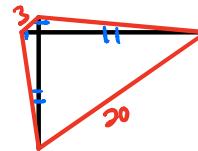
#8) If  $m\angle MTN = 116$ , find  $m\angle 1$  and  $m\angle 4$



$$\begin{aligned} m\angle 1 + m\angle 4 + 116 &= 180 \text{ (Angle Sum Th'm)} \\ 2m\angle 1 + 116 &= 180 \\ 2m\angle 1 &= 64 \\ m\angle 1 &= 32 \\ 116 &= m\angle 4 + m\angle 4 \text{ (Ext angle th'm)} \\ 116 &= 2m\angle 4 \\ 58 &= m\angle 4 \end{aligned}$$

Draw a counterexample to show that each statement below is false.

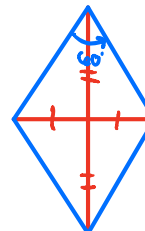
#9) If a quadrilateral has congruent diagonals, then it is a rectangle.



#10) If a quadrilateral has opposite sides congruent, then it is a rectangle.



#11) If a quadrilateral has diagonals that bisect each other, then it is a rectangle.



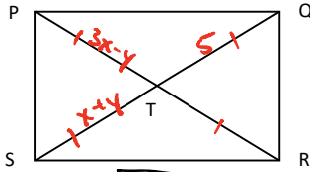
# Quadrilaterals – Rectangles

Homework Section 6.4

Name \_\_\_\_\_

Find the values of x and y in rectangle PQRS.

#12)  $PT = 3x - y$ ,  $ST = x + y$ ,  $TQ = 5$



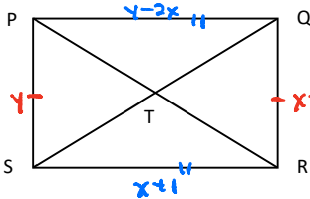
$PT = TQ$        $ST = TQ$   
 $3x - y = 5$        $x + y = 5$

$3x - y = 5$   
 $x + y = 5$

$3(5 - y) - y = 5$   
 $15 - 3y - y = 5$   
 $15 - 4y = 5$   
 $-4y = -10$   
 $y = \frac{5}{2}$   
 $x = \frac{5}{2}$

$(\frac{5}{2}, \frac{5}{2})$

#13)  $PS = y$ ,  $QR = x + 7$ ,  $PQ = y - 2x$ ,  $SR = x + 1$



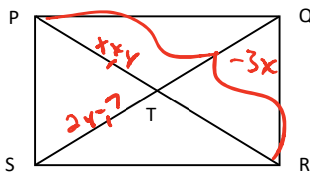
$PQ = SR$        $PS = QR$   
 $y - 2x = x + 1$        $y = x + 7$

$y - 2x = x + 1$   
 $y = x + 7$

$(x + 7) - 2x = x + 1$   
 $-x + 7 = x + 1$   
 $7 = 2x + 1$   
 $6 = 2x$   
 $3 = x$

$(3, 10)$

#14)  $PT = x + y$ ,  $ST = 2y - 7$ ,  $PR = -3x$



$ST = PT$        $PT + TR = PR$   
 $2y - 7 = x + y$        $(x + y) + (x + y) = -3x$   
 $y - 7 = x$        $2x + 2y = -3x$   
                           $2y = -5x$

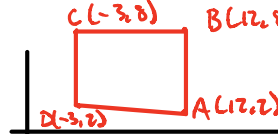
$y - 7 = x$   
 $2y = -5x$

$2y = -5(y - 7)$   
 $2y = -5y + 35$   
 $7y = 35$   
 $y = 5$

$(-2, 5)$

Determine whether ABCD is a rectangle. Explain

#15) A(12, 2), B(12, 8), C(-3, 8), D(-3, 2)



$m_{\overline{AB}} = \frac{\Delta y}{\Delta x} = \frac{(8) - (2)}{(12) - (12)} = \frac{6}{0} = \text{und vertical}$

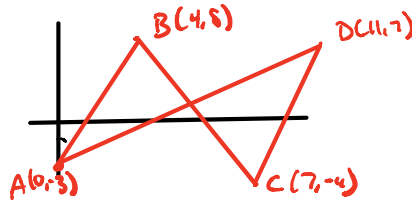
$m_{\overline{CD}} = \frac{\Delta y}{\Delta x} = \frac{(8) - (2)}{(-3) - (-3)} = \frac{6}{0} = \text{und vertical}$

$m_{\overline{BC}} = \frac{\Delta y}{\Delta x} = \frac{(8) - (8)}{(-3) - (12)} = \frac{0}{-15} = 0$  horizontal

$m_{\overline{AD}} = \frac{\Delta y}{\Delta x} = \frac{(2) - (2)}{(-3) - (12)} = \frac{0}{-15} = 0$  horizontal

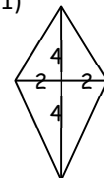
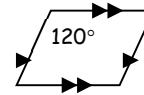
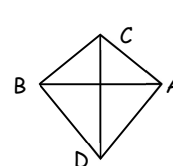
This is a rectangle because opposite sides are parallel and consecutive sides are  $\perp$ .

#16) A(0, -3), B(4, 8), C(7, -4), D(11, 7)



This is not a quadrilateral because so it can't be a rectangle.

- #1) 12      #2) 8      #3) 6
- #4) 62.5      #5) 70      #6) 32, 58, 58
- #7) 28.5      #8) 32, 58
- #9)  $CD = AB$       #10)      #11)



- #12) (2.5, 2.5)      #13) (3, 10)      #14) (-2, 5)
- #15) Yes, opposite sides are parallel and consecutive sides are parallel.  $\perp$
- #16) No, opposite sides are not parallel.