

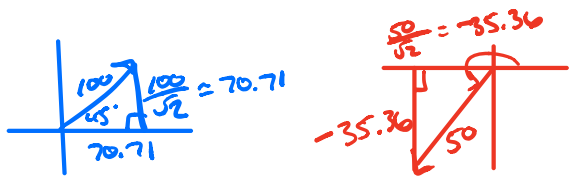
V7 - Find Resultant Vectors (More difficult problems)

Assume all angles are given in standard position.

1. George throws a headless doll 100 feet at an angle of 45° . Upon landing, George throws the doll again at 225° for 50 feet. What is the resulting vector in polar coordinates?

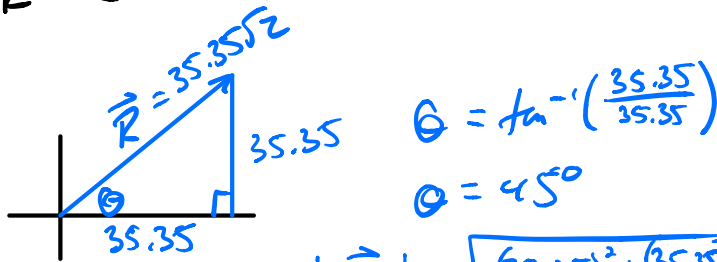
$$\vec{a} = (100, 45^\circ) \quad \vec{b} = (50, 225^\circ)$$

$$\vec{a} = \langle 70.71, 70.71 \rangle \quad \vec{b} = \langle -35.36, -35.36 \rangle$$



$$\vec{R} = \langle 70.71 - 35.36, 70.71 - 35.36 \rangle$$

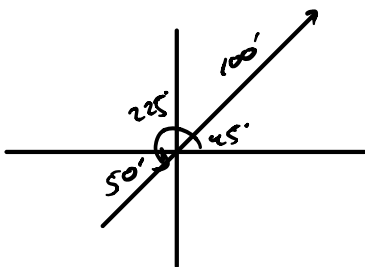
$$\vec{R} = \langle 35.35, 35.35 \rangle$$



$$\|\vec{R}\| = \sqrt{(35.35)^2 + (35.35)^2}$$

$$\|\vec{R}\| \approx 49.99$$

$$\vec{R} = (49.99, 45^\circ)$$



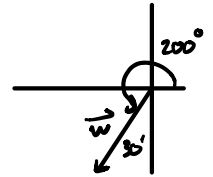
2. George throws a doll's head 25 feet at an angle of 140° . After running and picking it up, he throws the head again 30 feet at an angle of 200° . What is the resulting vector in polar coordinates?

$$x = r \cos \theta \quad y = r \sin \theta$$

$$x = 25 \cos(140^\circ) \quad y = 25 \sin(140^\circ)$$

$$x = -19.15 \quad y = 16.07$$

$$\vec{V} = \langle -19.15, 16.07 \rangle$$



$$\vec{W} = \langle r \cos \theta, r \sin \theta \rangle$$

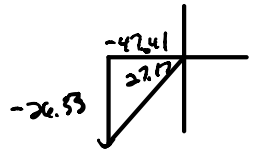
$$= \langle 30 \cos(200^\circ), 30 \sin(200^\circ) \rangle$$

$$\vec{W} = \langle -28.19, -10.26 \rangle$$

$$\vec{R} = \langle -19.15, 16.07 \rangle$$

$$+ \langle -28.19, -10.26 \rangle$$

$$\vec{R} = \langle -47.41, -26.33 \rangle$$



$$\vec{R} = (54.23, 207.17^\circ)$$

$$\|\vec{R}\| = \sqrt{(-47.41)^2 + (-26.33)^2}$$

$$\|\vec{R}\| = 54.23$$

$$\theta' = \tan^{-1}\left(\frac{26.33}{47.41}\right)$$

$$\theta' = 27.17^\circ$$

$$\theta = 180^\circ + 27.17^\circ$$

$$= 207.17^\circ$$