Venn Diagrams
That's Foreign to Me
In a class of 30 students, 19 are studying French, 12 are studying Spanish and 7 are studying both French and Spanish
P.1: Show the sample space
P.1: If you choose a student at random, what is the probability the student is not taking a foreign language?
P.3: What is the probability of choosing someone who isn't in French given that the person is in Spanish?
P.3: What is the probability of choosing a person who does not take Spanish, given that the person is in French?

## Concussed Boogers

On a football field of 22 players, 10 of the players have had a concussion, 15 of the players have picked their nose in public, and 8 of the players have had both a concussion and picked their nose in public.
P.1: Show the sample space
P.1: Ifyou choose a player at random, what is the probability that he has had a concussion only?

## P.3: Find $P(C \mid P)$

## P.3: Find $P(P \mid C)$

P.3: Find $P\left(P \mid C^{c}\right)$
P.3: Find $P\left(C \mid P^{c}\right)$

## Pool Party

You are having a pool party with 20 of your closest neighbors. As the host you serve watermelon and popsicles. 9 of your friends eat watermelon, 11 of your friends eat a popsicle and 5 ate nothing.

## P.1: Show the sample space

P.1: Ifyou choose a friend at random, what is the chance the friend ate both watermelon and a popsicle?
P.3: Find $P(P \mid W)$

## Gamification

There are 100 students in the sophomore class. Of these students, 25 own an Xbox, 50 own a Nintendo Switch and 40 don't own either.
P.1: Show the sample space
P.1: If you choose a student at random, what is the chance the student owns a Nintendo Switch only?
P.3: Find $P\left(X \mid N^{c}\right)$
P.3: Find $P\left(N^{c} \mid X^{c}\right)$

## Pets R Us

In a park of 85 people, 55 are walking a dog, 25 are walking a Paradoxasaur and 20 are not walking any animal.
P.1: Show the sample space
P.1: If you choose a person at random, what is the probability the person is walking both a dog and a Paradoxasaur?
P.3: Find $P(D \mid P)$
P.3: Find $P\left(P \mid D^{c}\right)$

## Binary Art

There are 10 types of people in this world, those who understand binary and those who don't. Of the 50 people in study hall, 22 of them are taking a computer course, 30 of them are taking an art class, and 15 are taking both a computer course and art class.
P.1: Show the sample space
P.1: If you choose a student at random, what is the chance the student only takes a computer class?
P.3: Find $P\left(A^{c} \mid C\right)$
P.3: Find $P\left(C^{c} \mid A\right)$

## End of Course Test Questions

The key to this section is on smacmathgeometry.weebly.com under "Air Test"

## 2018

## Question 18



## Tree Diagram

## A Kings Random

In a standard deck of 52 cards, you pick two cards at random. Find the chance of getting 2 Kings. Find the probability of picking a King on your first and not picking a King on your second. Find the probability of not picking a King on your first and picking a King on your second. Find the probability of both cards not being Kings.

## A Heart Returned

In a standard deck of 52 cards, you randomly pick a card, replace it, and randomly pick another card. Find the chance of getting 2 Hearts. Find the probability of picking a Heart on your first and not picking a Heart on your second. Find the probability of not picking a Heart on your first and picking a Heart on your second. Find the probability of both cards not being Hearts.

## Tricycle

You roll a die 3 times while riding a tricycle. What is the probability you get a 1 on each die? List the relevant sample space.

## Reds

In a standard deck of 52 cards, you are dealt two cards at random. Find the chance of getting 2 red cards. Find the probability of receiving red on your first and not receiving red on your second. Find the probability of receiving red on your first and receiving a red on your second. Find the probability of both cards not being red.

## Face Cards

In a standard deck of 52 cards, you pick two cards at random. Find the chance of getting 2 Face Cards. Find the probability of picking a Face Card on your first and not picking a Face Card on your second. Find the probability of not picking a Face Card on your first and picking a Face Card on your second. Find the probability of both cards not being Face Cards.

## One Eyed Jacks

In a standard deck of 52 cards, you randomly pick a card, replace it, and randomly pick another card. Find the chance of getting 2 One Eyed Jacks. Find the probability of picking a One Eyed Jack on your first and not picking a One Eyed Jack on your second. Find the probability of not picking a One Eyed Jack on your first and picking a One Eyed Jack on your second. Find the probability of both cards not being One Eyed Jacks.

## Pentacycle

A die is rolled 3 times while the rider is on a pentacycle. What is the probability at least one 5 landing up? List the relevant sample space.

## Reds

In a standard deck of 52 cards, you are dealt 5 cards. What is the probability that at least one card is a heart?

## State Released 1

An online retailer conducts a random survey of its customers. The survey shows that $80 \%$ of the customers receive their purchases within four days, $95 \%$ of those customers are satisfied with the quality of their purchases.

What percent of all customers receive their purchases within four days and are not satisfied with the quality of their purchases?
A) $4 \%$
B) $5 \%$
C) $19 \%$
D) $24 \%$
$\qquad$

## Two-Way Frequency Tables

Complete the two-way frequency tables.

1. Students were asked in Middle and High School which they liked more, Math or English. Complete the twoway table from the given information.

| Math | English | Total |  |
| :---: | :---: | :---: | :---: |
|  |  | 18 | 43 |
| Middle |  | 18 |  |
|  | 19 |  | 31 |
| Total |  |  | 74 |
|  |  |  |  |

2. Complete the two-way tables and determine the requested probability.

In the class of 24 boys and 10 girls a survey was given about whether they liked Justin Bieber or Katie Perry. 20 boys liked Katie Perry and 9 of the girls liked Justin Bieber. Complete the two-way table

3. A class of 35 students were asked if they were members of the chess club or math club. 16 were in the chess club, 10 were in both, 9 students weren't in either club.

$\mathrm{P}($ math club $)=$ $\qquad$
4. 15 boys and 20 girls were surveyed about music preference between Top 40 and 80 's music. 25 students picked Top 40 , and 2 girls picked 80 's music.

$P($ Boy and Top 40's $)=$ $\qquad$

Create the two-way tables.
5. High School freshman were surveyed about their use of Facebook and Twitter. Of the 80 freshman surveyed, 65 use Twitter, 69 use Facebook, and 62 use both. Create a two-way frequency table and then determine:

P(Not Twitter and Not Facebook) = $\qquad$

The boys and girls of a class were surveyed about whether The class had been surveyed about who had been to Canada, Europe or both. The two way table shows the

|  | Europe | Not Europe | Total |
| :---: | :---: | :---: | :---: |
| Canada | 3 | 22 | 25 |
| Not Been to | 2 | 7 | 9 |
| Total | 5 | 29 | 34 | results of the survey.

6. What is the probability that a student had been to Canada and Europe?
7. What is the probability that a student had been to Europe but not Canada?
8. What is the probability that a student had been to Canada?
9. Given that they had not travelled to Europe, what is the probability that they had been to Canada?

The boys and girls of a class had been surveyed about whether they had received a speeding ticket or not. The two way table shows the results of the survey.

|  | Speeding <br> Ticket |  | No Speeding <br> Ticket |
| :--- | :---: | :---: | :---: |
| Total |  |  |  |

10. What is the probability of getting a speeding ticket?
11. What is the probability of being a girl with a speeding ticket?
12. What is the probability that being a boy with no speeding ticket?
13. Who is more likely to getting a speeding ticket, boys or girls? Boys or Girls Explain your choice.
14. Are boys and speeding tickets independent or not? Yes or No
Use mathematics to explain your choice.
15. The town of Centerville is divided by a railroad track that splits the population of the town into two groups, the North side and South side of town. Centerville is having an election for the mayor; Tim Jenson is running against Joe Smith. If the side of town that you live on is independent of the candidate that you will choose, how many people do we expect on the North Side to vote for Joe Smith?


The following relative frequency table was created from the data gathered from a survey about favorite colors.

|  | Red | Blue Yellow Total |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Male | . 24 | . 14 | . 18 | 0 | . 56 |
| Female | . 16 | . 16 | . 06 | . 06 | . 44 |
| Total | . 40 | . 30 | . 24 | . 06 | 1 |

16. What is the $P($ Red $)$ ?
17. What is the P (Female)?
18. What is the $\mathrm{P}($ Green $\mid$ Male)?
19. What is the $P($ Female and Blue)?
20. What is the $P($ Red or Green $)$ ?
21. What is the $\mathrm{P}($ Male and Not Green)?
22. What is the $P$ (Blue or Female)?
$\qquad$

High Schools were surveyed about whether they owned a PS4 or an XBOX ONE. Of the 100 surveyed 70 owned XBOX ONE, 23 didn't own a PS4, and 9 didn't own either system.

23. What is the $\mathrm{P}($ No XBOX ONE)?
24. What is the P(PS4 | XBOX ONE)?
25. What is the $P(P S 4$ and $X B O X$ ONE)?
26. What is the $\mathrm{P}(\mathrm{PS} 4$ or XBOX ONE)?
27. What is the $P($ Neither System)?
30. A total of 50 students play either soccer or lacrosse.

20 girls play lacrosse.
20 boys play either soccer or lacrosse
20 students play soccer.
What is the probability that a student plays soccer or is a girl?
28. Are owning a PS4 and owning a XBOX ONE independent of each other? Yes or No Use mathematicsto explain your choice.
29. Why do you think that they two are not independent of each other? Why would one possibility influence the other?
32. Rosa collects data on what students at her school like to eat at the movie theater. She asks a random sample of 120 students two questions:

Do you like to eat popcorn at the movie theater?
Do you like to eat candy at the movie theater?
Her data are partially shown in the table. Of the students she asks, $60 \%$ of those who like to eat popcorn also like to eat candy.

Complete the table to show the number of students in each category.

|  | Like popcorn | Don't Like popcorn | Total |
| :--- | :--- | :--- | :--- |
| Like Candy |  |  | $\square$ |
| Don't Like Candy |  |  | 62 |
| Total |  |  |  |

Once the table above is complete, answer each questions.
33. What is the probability that a student likes candy?
34. What is the probability that a "don't like popcorn" was selected?
35. What is the probability that you select a person who likes candy that also likes popcorn?
36. Given that the person doesn't like candy, what is the probability they don't like popcorn?

## Review

## Probability

## End of Course Test Questions

The key to this section is on smacmathgeometry.weebly.com under "Air Test"

## 2017

## Question 4

During a 90 -day semester, a student records whether he arrives at school on time and whether he goes to bed by $10: 00 \mathrm{p} . \mathrm{m}$. the night before. The results are shown in the table.

## Number of Occurrences

|  | Arrives at School on Time | Arrives at School Late |
| :--- | :---: | :---: |
| Goes to Bed by 10:00 p.m. | 72 | 8 |
| Goes to Bed After 10:00 p.m. | 9 | 1 |

Does the student arriving at school on time depend on whether the student goes to bed by $10: 00 \mathrm{p} . \mathrm{m}$.? Justify your reasoning. Type your answer in the space provided.


2018

## Question 15

A total of 50 students play either soccer or lacrosse.

- 20 girls play lacrosse.
- 20 boys play either soccer or lacrosse.
- 20 students play soccer.

What is the probability that a student plays soccer or is a girl?
$\square$

## Question 9

An online retailer conducts a random survey of its customers. The survey shows that $80 \%$ of the customers receive their purchases within four days, and $95 \%$ of those customers are satisfied with the quality of their purchases.

What percent of all customers receive their purchases within four days and are not satisfied with the quality of their purchases?
(A) $4 \%$
(B) $5 \%$
(C) $19 \%$
(D) $24 \%$

## Question 11

Josh has a bag containing pieces of candy. The bag contains 10 red circular pieces, 10 red square pieces, 10 blue triangular pieces, and 10 blue star-shaped pieces. He draws a red piece of candy from the bag

What is the complement of this event?
(A) He draws a blue piece.
(B) He draws a square piece.
(c) He draws a circular piece.
(D) He draws a star-shaped piece.

## 2018

## Question 48

Rosa collects data on what students at her school like to eat at the movie theater. She asks a random sample of 120 students two questions:

- Do you like to eat popcorn at the movie theater?
- Do you like to eat candy at the movie theater?

Her data are partially shown in the table. Of the students she asks, $60 \%$ of those who like to eat popcorn also like to eat candy.
Complete the table to show the number of students in each category.

|  | Like Popcorn | Don't Like <br> Popcorn | Total |
| :---: | :---: | :---: | :---: |
| Like Candy |  |  | $\square$ |
| Don't Like Candy |  |  | 62 |
| Total | 70 |  | 120 |

## Question 5

A soccer coach determines that there is a $50 \%$ chance that a star player, Ralph, will play in a tournament.

- The probability that another star player, Dan, will play is 0.48 .
- The probability that both Ralph and Dan will play in the tournament is 0.25 .

Select phrases to complete the statement.
To find the probability that either Ralph or Dan will play in the tournament, first add $\quad$ and then

## Drop down choices

| To find the probability that either Ralph or Dan will play in the tournament, first |
| :--- |
| add |
| 0.50 and 0.48 <br> 0.50 and 0.25 <br> 0.48 and 0.25 |
| and then <br> subtract 0.25 from the sum. <br> multiply the sum by 0.48. <br> divide 0.50 by the sum. <br> subtract 0.50 from the sum. <br> multiply the sum by 0.25. <br> divide 0.48 by the sum. |

## Question 8

A survey was conducted to determine whether a group of 11th graders and 12th graders preferred to go to the amusement park or to the zoo for a class trip. The results are shown in the table.

|  | Amusement Park | Zoo |
| :--- | :---: | :---: |
| 11th Graders | 32 | 18 |
| 12th Graders | 24 | 26 |

Based on the table, what is the probability that a student preferred a class trip to the zoo given they are in 11th grade?

## Question 28

Bryan records the number of hours he sleeps each night for several days and whether it is raining in the morning when he wakes up. Bryan concludes that these two events are independent:

- Bryan sleeps 8 or more hours.
- It is raining in the morning.

Based on Bryan's conclusion, which statement must be true?
(A) Bryan never sleeps 8 or more hours on days that it is not raining in the morning.
(B) The probability that Bryan sleeps 8 or more hours is the same whether or not it is raining in the morning.
(c) The probability that Bryan sleeps 8 or more hours is influenced by whether or not it is raining in the morning.
(D) The probability that Bryan sleeps 8 or more hours is the same as the probability that it is raining in the morning.

## Question 32

A university determined the number of students pursuing different degrees, by gender. Some of the results are shown.

|  | Undergraduate <br> Degree | Master's <br> Degree | Doctoral <br> Degree | Total |
| :--- | :---: | :---: | :---: | :---: |
| Male |  |  | 500 | 12,500 |
| Female |  | 2,500 |  | 12,500 |
| Total | 16,250 | 6,250 | 2,500 | 25,000 |

What is the probability that a female student chosen at random is pursuing an undergraduate degree?
(A) $18 \%$
(B) $32 \%$
(c) $36 \%$
(D) $64 \%$

## Probability

1. Josh has a bag containing pieces of candy. The bag contains 10 red circular pieces, 10 red square pieces, 10 blue triangular pieces, and 10 blue star-shaped pieces. He draws a red piece of candy from the bag.

What is the complement of this event?
A) He draws a blue piece
B) He draws a square piece
C) He draws a circular piece
D) He draws a star-shaped piece
2. Given the spinner, what is the:
$P($ Red $)=$ $\qquad$
$P(\text { Red })^{c}=$ $\qquad$
$P($ White $)=$ $\qquad$

P(Green) = $\qquad$

$P(\text { Green })^{\mathrm{C}}=$ $\qquad$
$P($ Blue $)=$ $\qquad$
3. Given a bag of marbles, what is the:

$$
\mathrm{P}(\text { Black })=
$$

$P($ White $)=$ $\qquad$
$P($ Swirl $)=$ $\qquad$

$P(\text { Swirl })^{C}=$ $\qquad$
4. Sam is picking fruit from a basket that contains many different kinds of fruit. Which set is independent?
A) Event 1: He picks a kiwi and eats it

Event 2: He picks an apple and eats it
B) Event 1: He picks an apple and eats it

Event 2: He picks an apple and eats it
C) Event 1: He picks a kiwi and eats it Event 2: He picks a kiwi and puts it back
D) Event 1: He picks a kiwi and puts it back Event 2: He picks an apple and puts it back

## Chapter Review

5. Given the roll of 2 dice and their values are summed, what is the:


Complete the table of the sample space of the sum of two die.

$P($ sum of 12$)=$ $\qquad$
$P(\text { sum of } 12)^{c}=$ $\qquad$
$P($ sum of 7$)=$ $\qquad$
$P($ sum of 4$)=$ $\qquad$
$P(\text { sum of } 4)^{c}=$ $\qquad$
$P(\text { even sum })^{c}=$ $\qquad$
6. Joemomma is choosing cards from a deck of cards or rolls a die. Which set is independent?
A) Event 1: He picks a card and keeps it

Event 2: He picks a second card
B) Event 1: He picks a card and keeps it

Event 2: He rolls a die
C) Event 1: He picks a marble and keeps it

Event 2: He picks a second marble
D) Event 1: He picks a card and rips it up Event 2: He picks a second card
7. A total of 200 people attend a party, as shown in the table.

|  | Adults | Children | Total |
| :---: | :---: | :---: | :---: |
| Male |  |  | 80 |
| Female |  |  | 120 |
| Total | 150 | 50 | 200 |

A person is selected at random to win a prize. The probability of selecting a child, given that the person is female, is 0.25 . The probability of selecting a male, given that the person is a child, is 0.4 .

Complete the two-way table to show the number of adults, children, males, and females who attended the party.
8. Rosa collects data on what students at her school like to eat at the movie theater. She asks a random sample of 120 students two questions:

- Do you like to eat popcorn at the movie theater?
- Do you like to eat candy at the movie theater?

Her data are partially shown in the table. Of the students she asks, $60 \%$ of those who like to eat popcorn also like to each candy. Complete the table to show the number of students in each category.

|  | Like <br> Popcorn | Don't <br> Like <br> Popcorn | Total |
| :---: | :---: | :---: | :---: |
| Like <br> Candy |  |  |  |
| Don't Like <br> Candy |  |  | 62 |
| Total | 70 |  | 120 |

9. A total of 50 students play either soccer or lacrosse.

- 20 girls play lacrosse
- 20 boys play either soccer or lacrosse
- 20 students play soccer

What is the probability that a student plays soccer or is a girl?
10. Use the incomplete table to answer the questions below.
a. Complete the table.

|  | Adults | Children | Total |
| :---: | :---: | :---: | :---: |
| Male |  | 20 |  |
| Female |  |  | 60 |
| Total | 25 | 65 |  |

b. If a person is chosen at random, what is the probability the person is an adult and a male?
c. If a person is chosen at random, what is the probability the person is a child?
d. If a female is chosen at random, what is the probability the female is a child?
e. If a child is chosen at random, what is the probability the child is an adult and a female?
$\qquad$
11. The probability of flipping a fair coin and heads landing face up is 0.5 . The probability of rolling a fair number cube, with sides numbered 1 through 6 , and an odd number landing face up is 0.5 .

What is the probability of flipping heads up or rolling an odd number?
12. An online retailer conducts a random survey of its customers. The survey shows that $80 \%$ of the customers receive their purchases within four days, $95 \%$ of those customers are satisfied with the quality of their purchases.

What percent of all customers receive their purchases within four days and are not satisfied with the quality of their purchases?
E) $4 \%$
F) $5 \%$
G) $19 \%$
H) $24 \%$
13. Events $A$ and $B$ are independent.
$P(A$ and $B)=0.25$
What are possible probabilities for events $A$ and $B$ ?
$P(A)=$
$P(B)=$
14. During a 90-day semester, a student records whether he arrives at school on time and whether he goes to bed by $10: 00 \mathrm{pm}$ the night before. The results are shown in the table

| Number of Occurrences |  |  |
| :--- | :---: | :---: |
|  | Arrives at School <br> on Time | Arrives at School <br> Late |
| Goes to Bed by 10:00 pm | 72 | 8 |
| Goes to Bed After $10: 00 \mathrm{pm}$ | 9 | 1 |

Does the student arriving at school on time depend on whether the student goes to bed by 10:00 pm? Justify your reasoning.
15. The two-way table shows the number of births, in thousands, in the United States for the years 2010 and 2011.

|  | J a n | F | $\begin{aligned} & \mathrm{M} \\ & \mathrm{a} \\ & \mathrm{r} \end{aligned}$ | $\mathrm{A}$ | $\begin{aligned} & \mathrm{M} \\ & \mathrm{a} \\ & \mathrm{y} \end{aligned}$ | $\begin{aligned} & \mathrm{Ju} \\ & \mathrm{n} \\ & \mathrm{e} \end{aligned}$ | $\begin{aligned} & \mathrm{J} \\ & \mathrm{u} \\ & \mathrm{ly} \end{aligned}$ | $\begin{aligned} & \mathrm{A} \\ & \mathrm{u} \\ & \mathrm{~g} \end{aligned}$ | $\begin{aligned} & \mathrm{S} \\ & \mathrm{e} \\ & \mathrm{p} \end{aligned}$ | $\begin{aligned} & \mathrm{O} \\ & \mathrm{c} \\ & \mathrm{t} \end{aligned}$ | $\begin{aligned} & \mathrm{N} \\ & \mathrm{o} \\ & \mathrm{v} \end{aligned}$ | $\begin{aligned} & \mathrm{D} \\ & \mathrm{e} \\ & \mathrm{c} \end{aligned}$ | T ot al |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 4 |
| 0 | 2 | 0 | 4 | 2 | 2 | 3 | 4 | 5 | 5 | 4 | 3 | 2 | 0 |
| 1 | 4 | 3 | 0 | 7 | 5 | 8 | 6 | 9 | 0 | 2 | 7 | 6 | 1 |
| 0 |  |  |  |  |  |  |  |  |  |  |  |  | 7 |
| 2 | 3 | 2 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 |
| 0 | 2 | 9 | 3 | 1 | 2 | 3 | 4 | 6 | 4 | 3 | 2 | 2 | 9 |
| 1 | 2 | 9 | 0 | 5 | 8 | 5 | 8 | 2 | 6 | 1 | 8 | 2 | 6 |
| 1 |  |  |  |  |  |  |  |  |  |  |  |  | 6 |

A baby born in 2011 is randomly selected. What is the probability that the baby was born in February?
16. Fransisco asks the students in his school what pets they have. He studies the events show.

- Event S: The students has a cat.
- Event T: The students has a dog.

Fransisco finds that the two events are independent.
Select all the equations that must be true for events $S$ and T .

$$
\begin{array}{ll}
\circ & P(S \mid T)=P(S) \\
\circ & P(S \mid T)=P(T) \\
\circ & P(T \mid S)=P(S) \\
\circ & P(T \mid S)=P(T) \\
\circ & P(S \cup T)=P(S) \cdot P(T) \\
\circ & P(S \cap T)=P(S) \cdot P(T)
\end{array}
$$

17. Juan studies the events shown below.

- Event A: A student has hairy moles
- Event B:A student is born by the toxic waste plant
Juan find the $P(A \mid B)=P(A)$
What assumptions can be made about Event $A$ and Event B? Choose all that apply.
A. $A$ and $B$ are independent
B. A and $B$ are dependent
C. A and B are mutually exclusive
D. A and $B$ must happen together
E. A and B can't happen together

18. Timmy studies the events shown below.

- Event A: A student has no teeth
- Event B : A student is born in Midvale

Timmy finds the $P(A \cap B)=P(A) \cdot P(B)$
What assumptions can be made about Event $A$ and Event B? Choose all that apply.
A. $A$ and $B$ are independent
B. A and $B$ are dependent
C. A and B are mutually exclusive
D. A and B must happen together
E. A and B can't happen together
19. Max studies the events shown below.

- Event A: A student has no teeth
- Event $\mathrm{B}: \mathrm{A}$ student is born in Midvale

Timmy find the $P(B \mid A) \neq P(B)$
What assumptions can be made about Event $A$ and Event B? Choose all that apply.
A. $A$ and $B$ are independent
B. A and $B$ are dependent
C. A and $B$ are mutually exclusive
D. A and B must happen together
E. A and B can't happen together
20. This Venn diagram represents students who play instruments in the orchestra.


Identify each region of the Venn diagram that represents students who play only the flute and the oboe

Use this for the next 2 problems: The usher at a wedding asked each of the 80 guests whether they were a friend of the bride or of the groom. Here are the results:

21. In this sample, are the events "bride" and "groom" mutually exclusive?
22. Find the probability that a randomly selected person from this sample was a friend of the bride OR of the groom.

## Perimeter

Hw Section 14.1
Determine the circumference. Leave as an exact value.

1. $r=5 \sqrt{3}$
2. $\mathrm{d}=\frac{5}{4} \mathrm{~cm}$
3. 


8.

4. $r=\frac{11}{16} \mathrm{~cm}$, find C .

Determine the perimeter of the following figures.
(Lines that appear to be perpendicular are perpendicular.)
5.


12.

13.

15.


17.

18.

19.

20.


## Area of Parallelograms \& Triangles

## Draw the following. Find the area. Label your answer!

1. $\square Y E A H$ with base of 12 ft and $\quad$ 2. $\triangle Y E S$ with base 4.5 cm and altitude 3 . $4 \mathrm{ft} \times 8 \mathrm{ft}$ rectangle $Y E P S$. height of 9 ft . of 3 cm .
height or ft .

Find the area of each. Label you answer!

| 4. | 5. | 6. |
| :---: | :---: | :---: |
| 7. | 8. | 9. |
| 10. | 11. | 12. |

## Find the missing measurement. Round to the nearest tenth.



| ALGEBRA REVIEW |  |  |  |
| :---: | :---: | :---: | :---: |
| SOLVE $2(3-2 x)<35$ | $2 x+3 y=-9$ |  | $\begin{gathered} \text { MULTIPLY } \\ (2 x-5)(x+3) \end{gathered}$ |
| SOLVE $4 x+5 \geq 8+6 x$ | $4 x-2 y \leq 10$ | GRAPH | $\begin{gathered} \text { FACTOR } \\ 6 x^{2}-7 x-5 \end{gathered}$ |

## Draw the following. Find the area. Label your answer!

| 1. $\triangle Y E A H$ with a base of 12 ft, a base of 8 ft and |
| :--- | :--- |
| altitude of 9 ft. |$\quad$| 2. Kite $M A T H$ with a diagonal of 7.2 cm and a diagonal of |
| :--- |
| 10.4 cm. |

Find the area of each. Label your answer!


Find the missing measurement. Round to the nearest tenth.

## 11. TRAPEZOID



Area $=21 \mathrm{~m}^{2}$
12. KITE


Area $=182 \mathrm{~cm}^{2}$
13. TRAPEZOID


Area $=62.6 \mathrm{yd}^{2}$


| Find the area of each. Label you answer! |  |
| :--- | :--- |
| 1. | 2. <br> Nonagon <br> Apothem $=14 \mathrm{~cm}$ <br> Side $=8 \mathrm{~cm}$ |


| 5. | 6. |
| :--- | :--- |


6.

7.

8.


| Draw the following. Find the area. Label your answer! |  |
| :--- | :--- | :--- |
| 9. A square with apothem of 4 in and perimeter of 32 in. | 10. A regular pentagon with each side of 5 cm. |


| ALGEBRA REVIEW |  |  |  |
| :---: | :---: | :---: | :---: |
| SOLVE $5-2(3-2 x)<35$ | $3 y=2 x-9$ |  | $\begin{gathered} \text { MULTIPLY } \\ (2 x-5)(3 x+4) \end{gathered}$ |
| SOLVE $-4 x-5 \geq-11-6 x$ | $4 x+5 y \leq 10$ |  | $\begin{gathered} \text { FACTOR } \\ 2 x^{2}-x-3 \end{gathered}$ |

## Circles \& Arcs

Hw Section 14.5

Find the area. Give exact answer unless told otherwise.
1.


Determine the area of each sector. Give exact answers unless told otherwise.
5.

6.

3.

4.

8.


Determine the area of the following figures. Assume lines that appear perpendicular and parallel are in fact so.
9.

13.


14.


## End of Course Test Questions

The key to this section is on smacmathgeometry.weebly.com under "Air Test"

## 2018

## Question 29

Points A, B and C lie on a circle with center Q.

- The area of sector AQB is twice the area of sector BQC.
- The length of arc $A B$ is 28 centimeters.

What is the length, in centimeters, of arc $B C$ ?


## Question 36

To estimate the area of the circle, Henry divides a circle of radius $r$ into $n$ triangles, as shown, and uses the expression $\frac{h}{2}\left(b_{1}+b_{2}+\ldots+b_{n}\right)$ to estimate the area of the circle. In the expression, variables $b_{1}, b_{2}$, up to $b_{n}$ represent the base lengths of each triangle and $h$ represents the height of each triangle.


Henry claims that the more triangles the circle is divided into, the closer the estimated area will be to the actual area.

Which statement about Henry's claim is accurate?
(A His claim is accurate because as $n$ gets larger, the value of $h$ gets closer to the value of $r$ and the value of $\left(b_{1}+b_{2}+\ldots+b_{n}\right)$ approaches $2 \pi r$.
(B) His claim is accurate because as $n$ gets larger, the value of $h$ gets closer to the value of $2 r$ and the value of $\left(b_{1}+b_{2}+\ldots+b_{n}\right)$ approaches $\pi r$.
(c) His claim is inaccurate because as $n$ gets larger, the value of $h$ gets closer to the value of $r$ and the value of $\left(b_{1}+b_{2}+\ldots+b_{n}\right)$ deviates from $2 \pi r$.
(D) His claim is inaccurate because as $n$ gets larger, the value of $h$ gets closer to the value of $2 r$ and the value of $\left(b_{1}+b_{2}+\ldots+b_{r}\right)$ deviates from $\pi r$.

Determine the perimeter of the following figures. (Lines that appear to be perpendicular are perpendicular and lines that appear to be parallel are.)
1.

2.

3.


Determine the area of the following figures. (Lines that appear to be perpendicular are perpendicular and lines that appear to be parallel are.)
4.

5.

6.


8.

9.


11.

12.


14.


Determine the area of the circle or shaded circle sector.
15.

16.

17.

18.


Determine the area of the following figures. (Lines that appear to be perpendicular are perpendicular and lines that appear to be parallel are.)
19.

20.

21.


Find the area of each regular polygon.
22. Pentagon with an apothem of 4 cm
23. Equilateral triangle with a side of 6 cm .
24. Hexagon with a perimeter of 48 cm .

## Volume - Prisms

Hw Section 15.1

Determine the volume of the following prisms. (Lines that appear perpendicular are perpendicular.)

1. The same rectangular prism is provided three times below but in each instance a DIFFERENT BASE has been highlighted. Calculate the volume for each but change the base dimensions.

2 cm

2.

3.


5.

6. Regular Hexagonal Prism


8.

9.


11.

12.


## End of Course Test Questions

The key to this section is on smacmathgeometry.weebly.com under "Air Test"

## 2017

## Question 1

Triangle ABC is shown.


Which three-dimensional figure results from rotating the triangle $360^{\circ}$ about $\overline{\mathrm{AC}}$ ?
(A) cone
(B) cylinder
(C) pyramid
(D) sphere

## End of Course Test Questions

The key to this section is on smacmathgeometry.weebly.com under "Air Test"

## 2018

## Question 16

A cube is sliced as shown.


What is the shape of the cross section?
(A) Rectangle

(B) Rhombus

(c) Square

(D) Trapezoid


Volume - Cylinders \& Cones
Determine the volume of the following.
1.

2.

3.

4.


Hw Section 15.2

6. Square hole with sides of 3 cm


10.


## End of Course Released Questions

2019

## Question 1

A cylinder is sliced vertically along a dotted line, as shown.


Which two-dimensional shape is created from this cross section?
(A)

(c)

(B)

(D)


## Question 41

A company wants to design a cylindrical object that has a height of 10 centimeters and a volume of at least 2,000 cubic centimeters, but not more than 2,500 cubic centimeters.

What is a possible radius, in centimeters, of the cylinder? Round your answer to the nearest hundredth.


## Volume - Pyramids \& Spheres

Match the following terms to the diagram.
1.


Slant Height
$\qquad$
$\qquad$ Height
$\qquad$
$\qquad$ Face
$\qquad$ Vertex
2. Two pyramids with the same base are side by side. One is a right pyramid and the other is an oblique pyramid. If the oblique pyramid has been tilted to an angle of $80^{\circ}$, what is volume relationship between the two pyramids?


Hw Section 15.3
Determine the volume of the following.
3. Rectangular Pyramid


8. Square Pyramid



10


12. Two tennis balls fit exactly in the 48 cm tall cylindrical can. What is the volume of air in the can?


## End of Course Test Questions

The key to this section is on smacmathgeometry.weebly.com under "Air Test"

## 2017

## Question 5

A globe has a diameter of 12 inches. It fits inside a cube-shaped box that has a side length of 12 inches.
What is the volume, rounded to the nearest hundredth of a cubic inch, of the space inside the box that is not taken up by the globe?
cubic inches

## End of Course Test Questions

The key to this section is on smacmathgeometry.weebly.com under "Air Test"

## 2018

## Question 34

A cone and a sphere have the same volume. The height of the cone is 96 units.
What could be the values for the radius of the cone and the sphere? Round your answers to the nearest hundredth
as needed.
Radius of Cone:
Radius of Sphere:

## Perimeter, Area \& Volume

Determine the perimeter of the following figures. (Lines that appear to be perpendicular are perpendicular and lines that appear to be parallel are.)
1.

2.


Determine the area of the following figures. (Lines that appear to be perpendicular are perpendicular and lines that appear to be parallel are.)
3.

4.

5.

6.


8.

9.


Determine the area of the circle or shaded circle sector.
10.

11.

12.

$\qquad$

Determine the area of the following figures. (Lines that appear to be perpendicular are perpendicular and lines that appear to be parallel are.)
13.


Find the area of each regular polygon.
14. Pentagon with an apothem of 4 cm
15. Equilateral triangle with a side of 6 cm .
16. Hexagon with a perimeter of 48 cm .
17. The volume of a rectangular prism with base dimensions of 3 cm and 8 cm and a prism height of 12 cm is:
A. $132 \mathrm{~cm}^{3}$
B. $144 \mathrm{~cm}^{3}$
C. $288 \mathrm{~cm}^{3}$
D. $576 \mathrm{~cm}^{3}$
18. The volume of a triangular prism with base dimensions of 4 cm height and 10 cm base and a prism height of 15 cm is:
A. $150 \mathrm{~cm}^{3}$
B. $300 \mathrm{~cm}^{3}$
C. $600 \mathrm{~cm}^{3}$
D. $900 \mathrm{~cm}^{3}$
19. The volume of a square pyramid with a base edge of 4 cm and a pyramid height of 9 cm is:
A. $144 \mathrm{~cm}^{3}$
B. $72 \mathrm{~cm}^{3}$
C. $48 \mathrm{~cm}^{3}$
D. $36 \mathrm{~cm}^{3}$
20. The volume of a sphere with a radius of 3 cm is:
A. $9 \pi \mathrm{~cm}^{3}$
B. $12 \pi \quad \mathrm{~cm}^{3}$
C. $36 \pi \mathrm{~cm}^{3}$
D. $72 \pi \mathrm{~cm}^{3}$
21. The volume of a sphere with a diameter of 12 cm is:
A. $2304 \pi \mathrm{~cm}^{3}$
B. $288 \pi \mathrm{~cm}^{3}$
C. $144 \pi \mathrm{~cm}^{3}$
D. $72 \pi \mathrm{~cm}^{3}$

Determine the volume of the following solids. (Lines that appear to be perpendicular are perpendicular and lines that appear to be parallel are.).
22.

25.

26.

$\qquad$

## Trigonometric Functions - Degree Angles

Draw an angle with the given measure in standard position.


Find the measure of each angle.


State the quadrant in which the terminal side of each angle lies.

| $9 .-446^{\circ}$ | $10.870^{\circ}$ | $12.215^{\circ}$ |
| :--- | :--- | :--- | :--- |


| Find a coterminal angle between $\mathbf{0}^{\circ}$ and $\mathbf{3 6 0}{ }^{\circ}$. |  |
| :--- | :--- |
| $15 .-45^{\circ}$ | $16.435^{\circ}$ |
|  |  |
|  |  |

## Find ALL coterminal angles.



Determine if the statement is true or false. If it is false, give a counterexample.
28. If the terminal side of an angle in standard position lies in quadrant $I$, then the angle is positive.
29. If the initial and terminal sides of an angle coincide, then the measure of the angle is zero.

| Skillz Review Simplify the following. |  |  |  |
| :--- | :--- | :--- | :--- |
| 1. $\frac{\frac{1}{2}}{\frac{3}{4}}$ | 2. $\frac{\frac{1}{2}}{\frac{\sqrt{3}}{4}}$ | 3. $\left.\frac{3}{\left(\frac{\sqrt{3}}{4}\right.}\right)$ | 4. $\frac{\left(\frac{\sqrt{3}}{4}\right)}{\sqrt{2}}$ |

Draw an angle with the given measure in standard position.


State the quadrant in which the terminal side of each angle lies.

| $9 . \frac{15 \pi}{4}$ | $10 . \frac{5 \pi}{6}$ | $11 .-\frac{10 \pi}{9}$ | $12 .-\frac{17 \pi}{6}$ |
| :--- | :--- | :--- | :--- |

Find one positive and one negative coterminal angle the angle given. (IN RADIANS!)
13. $\frac{\pi}{3}$
Find a coterminal angle between 0 and $2 \pi$.
14. $\frac{5 \pi}{4}$
15. $\frac{9 \pi}{4}$
16. $\frac{13 \pi}{2}$

| $19.225^{\circ}$ | $20.280^{\circ}$ |
| :--- | :--- |
| $21 .-210^{\circ}$ | $22 .-1020^{\circ}$ |
|  |  |

Convert each radian measure into degrees.

| $23 .-\frac{5 \pi}{9}$ | $24 . \frac{5 \pi}{6}$ |
| :--- | :--- |
| $25 . \frac{23 \pi}{36}$ | $26 \cdot \frac{79 \pi}{18}$ |

3. Some people really freak out when they see an angle measurement in radians without pi. Don't freak out! Remember pi is just a number, so think of $\pi$ as $3.14, \frac{\pi}{2}$ as 1.57 , etc...

Draw the angle with the given radian measure in standard position.
a. 2

b. -1.2

c. 5


## Trigonometry - Reference Triangle

| Find the RATIO of the trig function indicated. Do NOT find the actual measure of the angle! |  |  |  |
| :---: | :---: | :---: | :---: |
| 1. | 2. | 3. | 4. |
| 5. | 6. $\cos \theta$ | 7. | 8. |



Draw the reference triangle. Find the EXACT value of the trig ratio for $\boldsymbol{\theta}$.

| 11. $\sin \theta$ for $(6,8)$ | $12 \cdot \cos \theta$ for $(\sqrt{3},-1)$ |
| :--- | :--- |
|  |  |

13. $\tan \theta$ for $(-15,-5) \quad 14 \sin \theta$ for $(-2,2 \sqrt{3})$

## Draw the reference triangle. Find the EXACT value of the trig ratio for $\boldsymbol{\theta}$.

| 15. Given $\tan \theta=\frac{12}{5}$ in quadrant III. <br> Find $\sin \theta$ | 16. Given $\cos \theta=-\frac{4}{5}$, where $\frac{\pi}{2}<\theta<\pi$. Find $\tan \theta$ |
| :--- | :--- |
|  |  |
| 17. Given $\tan \theta=-\frac{15}{8}$ where $\sin \theta<0$. | Find $\cos \theta$. <br> Fing $\sin \theta$ |

Find the exact value of the other 2 trig functions for angle $\theta$ in standard position.
19. $\tan \theta=3$ in quadrant III $\quad 20 . \sin \theta=\frac{3}{5}$ in quadrant II

## Trigonometry - Reference \& Special Angles Hw Section 16.4

| Find the reference angle. |  |  |  |
| :---: | :---: | :---: | :---: |
| 1. | 2. | 3. | 4. |
| 5. $-130^{\circ}$ | 6. $230^{\circ}$ | 7. $-\frac{13 \pi}{9}$ | 8. $\frac{3 \pi}{4}$ |

## Find the exact value.

| 9. $\sin 90^{\circ}=$ | $10 \cdot \cos 120^{\circ}=$ | $11 \cdot \tan 45^{\circ}=$ |
| :--- | :--- | :--- |
| $12 \cdot \tan 120^{\circ}=$ | $13 \cdot \cos 225^{\circ}=$ | $14 \cdot \sin 135^{\circ}=$ |
| $15 \cdot \sin 330^{\circ}=$ | $16 \cdot \tan 315^{\circ}=$ | $17 \cdot \cos 240^{\circ}=$ |
| $18 \cdot \sin \left(-225^{\circ}\right)=$ | $19 \cdot \cos \left(-240^{\circ}\right)=$ | $20 \cdot \tan \left(-300^{\circ}\right)=$ |

Find the exact value.

| 24. $\sin \frac{\pi}{2}=$ | 25. $\tan \frac{\pi}{4}=$ | $26 \cdot \cos \frac{3 \pi}{2}=$ |
| :--- | :--- | :--- |
| 27. $\cos \frac{4 \pi}{3}=$ | $28 \cdot \cos \frac{\pi}{6}=$ | $29 \cdot \tan \pi=$ |
| 30. $\sin \frac{5 \pi}{4}=$ | $31 \cdot \cos \frac{5 \pi}{3}=$ | $32 \cdot \sin \frac{5 \pi}{6}=$ |
| 33. $\tan \frac{7 \pi}{4}=$ | $34 \cdot \sin (-\pi)=$ | $35 \cdot \tan \left(-\frac{3 \pi}{2}\right)=$ |
| 36. $\cos \left(-\frac{\pi}{3}\right)=$ |  | $38 \cdot \sin \left(-\frac{5 \pi}{4}\right)=$ |


| If $\mathbf{0}^{\circ} \leq \boldsymbol{\theta} \leq 360^{\circ}$, then find $\boldsymbol{\theta}$ |  |  |  |
| :---: | :---: | :---: | :---: |
| 39. $\sin \theta=\frac{1}{2}$ | 40. $\cos \theta=\frac{\sqrt{3}}{2}$ | 41. $\tan \theta=-\sqrt{3}$ | If you like pictures of circles, you can draw one here! |
| 42. $\sin \theta=\frac{\sqrt{2}}{2}$ | 43. $\cos \theta=-\frac{\sqrt{2}}{2}$ | 44. $\tan \theta=-\frac{\sqrt{3}}{3}$ |  |
|  |  |  |  |
| If $0 \pi \leq \theta \leq 2 \pi$, then find $\theta$ |  |  |  |
| 48. $\sin \theta=\frac{\sqrt{3}}{2}$ | 49. $\tan \theta=1$ | 50. $\cos \theta=\frac{\sqrt{2}}{2}$ | If you like pictures of circles, you can draw one here! |
| 51. $\cos \theta=-\frac{1}{2}$ | 52. $\tan \theta=\sqrt{3}$ | 53. $\cos \theta=0$ |  |
|  |  | 56. $\sin \theta=-\frac{1}{2}$ |  |

57. Fill in the table below.


| - degree | - radian |
| :---: | :---: |
|  |  |

58. Fill in the table below.


| degrees | radians | $\sin \theta$ | $\cos \theta$ | $\tan \theta$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | -degree |
| - radian |  |  |  |  |  |  |  |

$\qquad$

## Trigonometry

## Review

Complete the coordinates for the unit circle.


Find the exact value.

| 9. $\sin 90^{\circ}=$ | 10. $\cos 120^{\circ}=$ | 11. $\tan 45^{\circ}=$ |
| :--- | :--- | :--- |
| $12 \cdot \tan 120^{\circ}=$ | 13. $\cos 225^{\circ}=$ | 14. $\sin 135^{\circ}=$ |
| $15 \cdot \sin 330^{\circ}=$ | 16. $\tan 315^{\circ}=$ | 17. $\cos 240^{\circ}=$ |
| $18 \cdot \sin \left(-225^{\circ}\right)=$ | 19. $\cos \left(-240^{\circ}\right)=$ | 20. $\tan \left(-300^{\circ}\right)=$ |

## If $0^{\circ} \leq \theta \leq 360^{\circ}$, then find $\theta$

| 39. $\sin \theta=\frac{1}{2}$ | 40. $\cos \theta=\frac{\sqrt{3}}{2}$ | 41. $\tan \theta=-\sqrt{3}$ |
| :--- | :--- | :--- |
| 42. $\sin \theta=\frac{\sqrt{2}}{2}$ | 43. $\cos \theta=-\frac{\sqrt{2}}{2}$ | 44. $\tan \theta=-\frac{\sqrt{3}}{3}$ |

State the quadrant in which the terminal side of each angle lies.

| 9. $-446^{\circ}$ | $10.870^{\circ}$ | $12.215^{\circ}$ |
| :--- | :--- | :--- | :--- | :--- |
| Find one positive and one negative coterminal angle the angle given. |  |  |
| 13. $30^{\circ}$ |  |  |

Draw the reference triangle. Find the EXACT value of the trig ratio for $\theta$.

| 11. $\sin \theta$ for $(6,8)$ | $12 \cdot \cos \theta$ for $(\sqrt{3},-1)$ |
| :--- | :--- |

13. $\tan \theta$ for $(-15,-5) \quad 14 \sin \theta$ for $(-2,2 \sqrt{3})$
